

Radar Equation “Cheat Sheet”

Dead Zone	$(ct)/2$
Range Resolution	$\Delta R = ct/2$
PRF	Pulse Repetition Frequency
PRI	Pulse Repetition Interval = 1/PRF
Unambiguous range	$c/(2PRF)$
Doppler shift	$f_d = \frac{2V_r}{\lambda}$
Unambiguous velocity	$V_{\max} = \frac{\lambda PRF}{4}$
Doppler dilemma	$V_{\max} R_{\max} = \frac{c\lambda}{8}$
Definition of radar reflectivity h ($m^2 m^{-3}$)	$h = \sum_{\text{Unit Volume}} s_i$
Radar reflectivity h ($m^2 m^{-3}$)	$s_i = V \sum_{\text{Unit Volume}} s_i = Vh$
Definition of radar reflectivity factor z (mm^6/mm^3)	$z = \sum_{\text{Unit Volume}} D^6$
Radar equation with incorporating simplified “lobing”	$P_r = \frac{G^2 I^2 P_t S}{64 p^3 R^4} \times 16 \sin^4 \left(\frac{2ph_a h_t}{IR} \right)$
Radar equation with incorporating simplified “lobing” in region below first peak	$P_r \approx \frac{4pP_t G^2 S (h_a h_t)^4}{I^2 R^8}$
Definition of refractivity	$N = (n-1) \cdot 10^6$ where n is the index of refraction
Distance to horizon (linear model of refractivity)	$d = \sqrt{2k a h_a}$ (Consistent Units) $d(km) = 4.12 \sqrt{h_a}$ (m) where a = diameter of earth, h_a is the antenna height and $k = 4/3$
Speed of radio wave	$c = \sqrt{\frac{m}{e}} = \sqrt{\frac{m_0}{e_0}} \sqrt{\frac{m_r}{e_r}} = c \sqrt{\frac{u_r}{e_r}} \propto c \sqrt{\frac{1}{e_r}}$

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General Antenna Formulas

G = Antenna Gain

λ = Wavelength (m)

$$A_e = \frac{G\lambda^2}{4\pi} \quad \text{Antenna Effective Area (m}^2\text{)}$$

$$G = \frac{4\pi k^2}{\theta \phi} \quad \theta, \phi \text{ are H and V beamwidths (radians), } k \text{ antenna factor}$$

$$G = \frac{4\pi}{\theta^2} \quad \text{For circular antennas, } \theta \text{ beamwidth (radians)}$$

Parabolic Dish Antennas

$$\theta = \frac{70\lambda}{D} \quad \text{Beamwidth in degrees, } D = \text{dish diameter} \quad \theta = \frac{\lambda}{D} \quad \text{Beamwidth in radians}$$

Radar Equation for Point Targets

$$P_r = \frac{G^2 \lambda^2 P_t \sigma}{64\pi^3 R^4}$$

P_t and P_r are transmitted and received power, σ is the radar target cross sectional area, R is the distance between target and transmitter, and G is the antenna gain.

Radar Equation for Distributed Targets

$$P_r = \frac{G^2 \lambda^2 P_t V \sigma}{64\pi^3 R^4}$$

P_t is the transmitted and received power, σ is the radar target cross sectional area, R is the distance between target and transmitter, and G is the antenna gain. V is the radar pulse volume (see below)

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Radar Pulse Volumes

$V_1 = p \frac{Rq}{2} \frac{Rf}{2} \frac{h}{2} \text{ (general)}$ $V_2 = \frac{pR^2 q^2 h}{8} \text{ (symetric } q = j \text{)}$ $V_3 = \frac{pR^2 qj}{8 \ln(2)} \frac{h}{2} \text{ (symectric, Gaussian)}$	<p>h = pulse length, t is the pulse width, q, and f are antenna beam widths.</p>
$P_r = \left(\frac{G^2 I^2 P_t q f c t}{1024 \ln(2) p^2} \right) \frac{h}{R^2} = C \frac{h}{R^2}$	<p>Radar equation for distributed targets using symmetric Gaussian antenna. C is the radar constant.</p>

Attenuation of electromagnetic energy in the atmosphere. Solid curve is due to absorption by oxygen. Dashed curve is due to absorption by water vapor.

