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1. Curved wall ABC in Figure 1 is a quarter circle 9 ft wide (into the paper). Compute the (a) horizontal  $F_H$  and (b) vertical  $F_V$  hydrostatic forces on the wall and (c) the line of action (i.e., the angle  $\theta$ ) of the resultant force  $F_R$ . ( $\gamma_{\text{water}} = 62.4 \text{ lb/ft}^3$ )

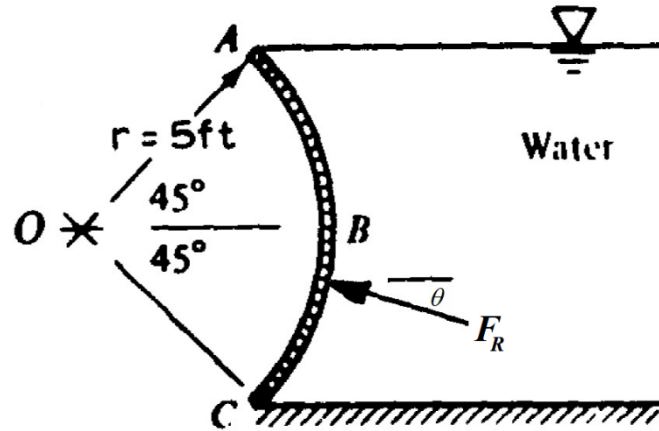


Figure 1

2. For the frictionless cart in Figure 2, compute (a) the  $x$ -component of the force on the wheels,  $F_x$ , caused by deflecting the water jet ( $\rho = 998 \text{ kg/m}^3$ ) and (b) the compression of the spring,  $\Delta x$ , if its stiffness is  $k = 1.6 \text{ kN/m}$ . For part (b), use the Hook's law,  $F_x = -k\Delta x$ . Assume steady state and circular cross sectional area for the water jet.

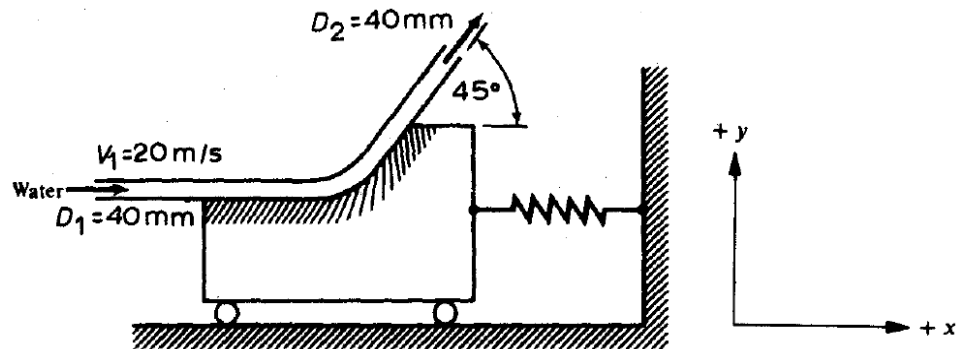


Figure 2

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3. The pressure rise,  $\Delta p$ , across a centrifugal pump in Figure 3(a) can be expressed as  $\Delta p = f(D, \omega, \rho, Q)$ , where  $D$  is the impeller diameter,  $\omega$  the angular velocity of the impeller (unit for  $\omega$  is  $T^{-1}$ ),  $\rho$  the fluid density, and  $Q$  the volume rate of flow through the pump. (a) By using dimensional analysis, show that the two pi terms of this problem are  $\Pi_1 = \Delta p / \rho \omega^2 D^2$  and  $\Pi_2 = Q / \omega D^3$ . (b) A model pump having a diameter of 8 in. is tested in a laboratory using water ( $\rho = 998 \text{ kg/m}^3$ ). When operated at an angular velocity of  $40\pi \text{ rad/s}$  the model pressure rise as a function of  $Q$  is shown in Figure 3(b). Use this curve to predict the pressure rise across a geometrically similar pump (prototype) for a prototype flowrate of  $6 \text{ ft}^3/\text{s}$ . The prototype has a diameter of 12 in. and operates at an angular velocity of  $60\pi \text{ rad/s}$ . The prototype fluid is also water.

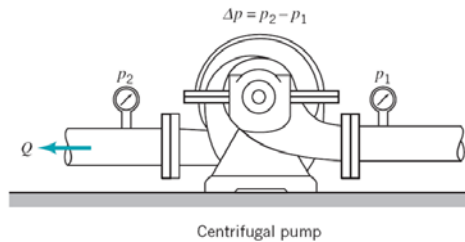


Figure 3(a)

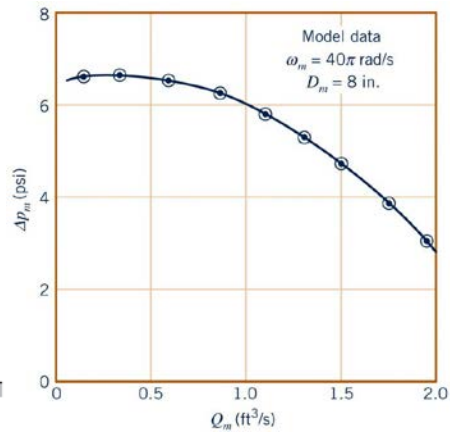


Figure 3(b)

4. If the pump shown in Figure 4 adds a head of 52 ft, determine the flow rate  $Q$  for the system. Do not neglect minor losses. Assume  $f = 0.01$  as your first guess then use the equation below for the remaining iterations until  $f$  converges to the thousandth decimal place. (Note:  $1 \text{ psi} = 144 \text{ lbf/ft}^2$ ,  $g = 32.2 \text{ ft/s}^2$ ,  $\rho = 1.94 \text{ slugs/ft}^3$ ,  $\mu = 2.34 \times 10^{-5} \text{ lbf} \cdot \text{s/ft}^2$ ,  $\gamma = 62.4 \text{ lbf/ft}^3$ ,  $\varepsilon = 0.00016 \text{ ft}$  and  $D = 2 \text{ ft}$ )

$$\frac{1}{\sqrt{f}} = -1.8 \log \left[ \left( \frac{\varepsilon/D}{3.7} \right)^{1.11} + \frac{6.9}{Re} \right]$$

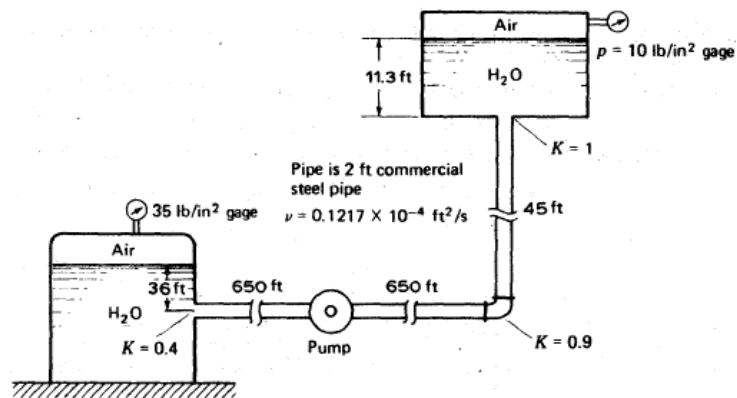


Figure 3

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5. The fixed keel of a Columbia 22 sailboat is about 38 in long as shown in Figure 5. Moving in Lake Ontario at a speed of (a) 2 knots and (b) 10 knots, what is the skin friction drag  $D_f$  from the keel, respectively? The water is at 40°F ( $\nu = 1.664 \times 10^{-5}$  ft<sup>2</sup>/s and  $\rho = 1.94$  slugs/ft<sup>3</sup>). Solve this problem using rectangular plate of length 38 in and width 24.5 in, which is the average width of the keel. Transition takes place at Reynolds number of  $5 \times 10^5$ . Note: 1 knot = 1.689 ft/s. See the Appendix A at the end of this exam for the friction drag coefficient,  $C_f$ .

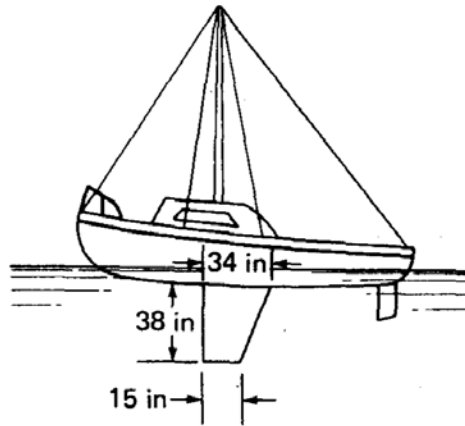


Figure 5

6. A heavy sphere attached to a string should hang at an angle  $\theta$  when immersed in a stream of velocity  $U$ , as shown in Figure 6(a). Knowing that the sphere should hang so that the string tension  $T$  balances the resultant of drag and net weight as shown in Figure 6(b), find (a) the net weight  $W$ , (b) the drag, and (c) the angle  $\theta$  if the sphere is steel ( $\rho_s = 7,844$  kg/m<sup>3</sup>) and diameter 3 cm and the flow is sea-level standard air ( $\rho_{air} = 1.225$  kg/m<sup>3</sup> and  $\mu_{air} = 1.78 \times 10^{-5}$  kg/m-s) at  $U = 40$  m/s. (Volume  $V = \pi D^3/6$  for a sphere of diameter  $D$ ). Neglect the string drag and the buoyancy force on the sphere, and use the Appendix B of this exam for the drag coefficient  $C_D$  if necessary.

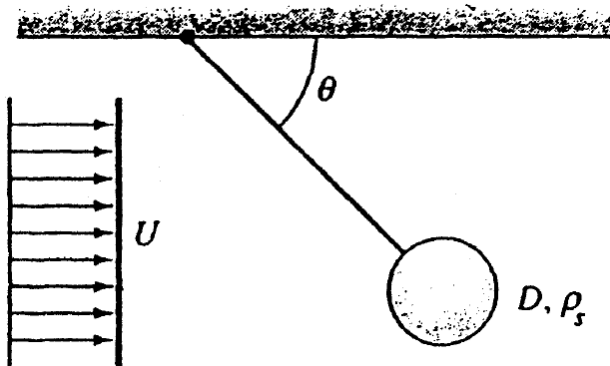


Figure 6(a)

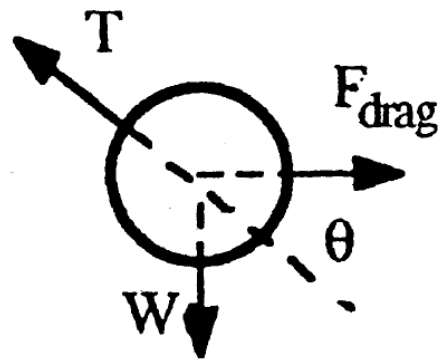
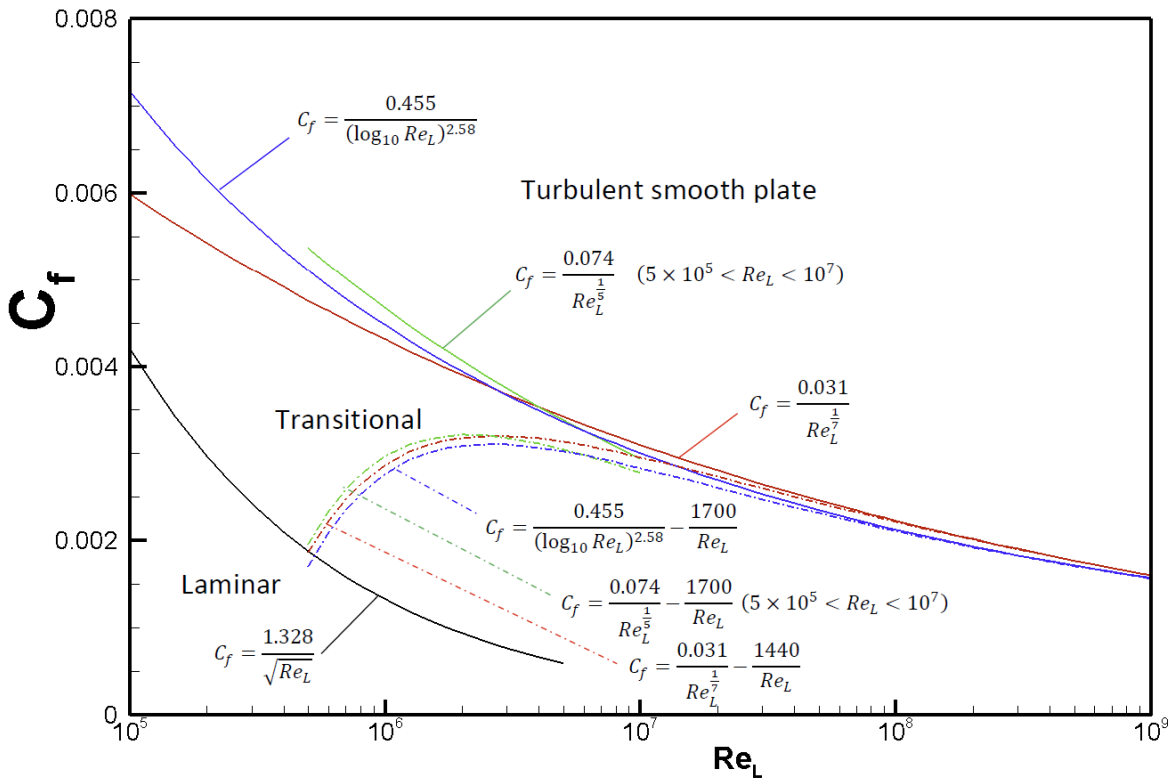


Figure 6(b)

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Appendix A. Friction drag coefficient for flat plate



Appendix B. Drag coefficient for a smooth sphere and a smooth cylinder

