

8.98

8.98 Water is circulated from a large tank, through a filter, and back to the tank as shown in Fig. P8.98. The power added to the water by the pump is 200 ft · lb/s. Determine the flowrate through the filter.

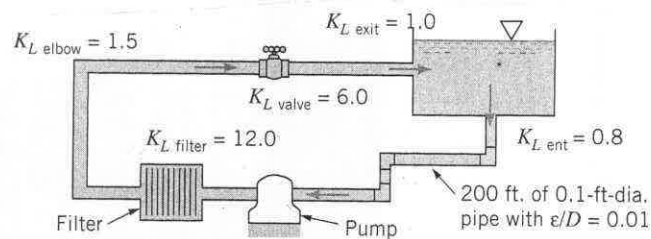


FIGURE P8.98

$$\frac{p_1}{\gamma} + z_1 + \frac{V_1^2}{2g} + h_p = \frac{p_2}{\gamma} + z_2 + \frac{V_2^2}{2g} + \left(f \frac{L}{D} + \sum_i K_{L_i} \right) \frac{V^2}{2g} \quad (1)$$

where

$$p_1 = p_2, \quad V_1 = V_2 = 0, \quad \text{and} \quad z_1 = z_2$$

$$\text{Also, } \dot{W}_p = \gamma Q h_p \text{ or}$$

$$h_p = \frac{200 \frac{\text{ft} \cdot \text{lb}}{\text{s}}}{62.4 \frac{\text{lb}}{\text{ft}^3} \left(\frac{\pi}{4} (0.1 \text{ ft})^2 \right) V} = \frac{408}{V}$$

Thus, Eq. (1) becomes

$$\frac{408}{V} = \left(\frac{200 \text{ ft}}{0.1 \text{ ft}} f + (0.8 + 5(1.5) + 12 + 6 + 1) \right) \frac{V^2}{2(32.2 \frac{\text{ft}}{\text{s}^2})}$$

$$\text{or} \quad V^3 = \frac{13.13}{(f + 0.01365)} \quad (2)$$

$$\text{Also, } Re = \frac{\rho V D}{\mu} = \frac{1.94 \frac{\text{slugs}}{\text{ft}^3} (V \frac{\text{ft}}{\text{s}}) (0.1 \text{ ft})}{2.34 \times 10^{-5} \frac{\text{lb} \cdot \text{s}}{\text{ft}^2}} \text{ or } Re = 8290V \quad (3)$$

Trial and error solution:

Assume $f = 0.04$. From Eq. (2), $V = 6.26 \frac{\text{ft}}{\text{s}}$; from Eq. (3), $Re = 5.20 \times 10^4$. Thus, from Fig. 8.20, $f = 0.039 \neq 0.04$

Assume $f = 0.039$, or $V = 6.29 \frac{\text{ft}}{\text{s}}$ and $Re = 5.21 \times 10^4$ and $f = 0.039$
(Checks)

$$\text{Thus, } Q = AV = \frac{\pi}{4} (0.1 \text{ ft})^2 (6.29 \frac{\text{ft}}{\text{s}}) = \underline{\underline{0.0494 \frac{\text{ft}^3}{\text{s}}}}$$

Alternatively, the Colebrook equation (Eq. 8.35) could be used rather than the Moody chart. Thus,

(cont)

8.98 (cont)

$$\frac{1}{\sqrt{f}} = -2.0 \log\left(\frac{\epsilon/D}{3.7} + \frac{2.51}{\text{Re}\sqrt{f}}\right), \text{ where from Eq.(2),} \quad (4)$$

$$f = (13.13/V^3) - 0.01365 \quad (5)$$

Thus, by combining Eqs. (3), (4), and (5) we obtain the following equation for V :

$$1/[(13.13/V^3) - 0.01365]^{1/2} = -2.0 \log\left[\frac{0.01}{3.7} + 2.51/[8290V][(13.13/V^3) - 0.01365]^{1/2}\right] \quad (6)$$

Using a computer root-finding program gives the solution to Eq.(6) as

$$V = 6.29 \frac{\text{ft}}{\text{s}}, \text{ the same as obtained by the above trial and error method.}$$