53:139 Foundation Engineering Department of Civil & Environmental Engineering The University of Iowa Supplement to Assignment #7

For a vertical retaining wall of height H and a sloping granular backfill of unit weight γ and friction angle φ , making angle α with respect to the horizontal, the resultant Rankine active and passive forces acting on the wall are given by the following relations:

$$P_{a} = \frac{\gamma H^{2}}{2} \cos \alpha \left[\frac{\cos \alpha - (\cos^{2} \alpha - \cos^{2} \phi)^{1/2}}{\cos \alpha + (\cos^{2} \alpha - \cos^{2} \phi)^{1/2}} \right]$$

$$P_{p} = \frac{\gamma H^{2}}{2} \cos \alpha \left[\frac{\cos \alpha + (\cos^{2} \alpha - \cos^{2} \phi)^{1/2}}{\cos \alpha - (\cos^{2} \alpha - \cos^{2} \phi)^{1/2}} \right]$$

The resultant forces act parallel to the sloping granular backfill that makes angle α with respect to the horizontal. **Derive both of these results using fundamental principles**.

